



Article

A Site Amplification Model for Crustal Earthquakes

M. Abdullah Sandıkkaya * and L. Doğan Dinsever

Civil Engineering Department, Hacettepe University, Ankara 06800, Turkey; latifdinsever999@gmail.com * Correspondence: abdullahsandikkaya@hacettepe.edu.tr; Tel.: +90-312-780-5829

Received: 19 February 2018; Accepted: 12 July 2018; Published: 17 July 2018



Abstract: A global dataset which is composed of more than 20,000 records is used to develop an empirical nonlinear soil amplification model for crustal earthquakes. The model also includes the deep soil effect. The soil nonlinearity is formulated in terms of input rock motion and soil stiffness. The input rock motion is defined by the pseudo-spectral acceleration at rock site condition (PSA_{rock}) which is also modified with between-event residual. Application of PSA_{rock} simplifies the usage of the site model by diminishing the need of using the period-dependent correlation coefficients in hazard studies. The soil stiffness is expressed by a Gompertz sigmoid function which restricts the nonlinear effects at both of the very soft soil sites and very stiff soil sites. In order to surpass the effect of low magnitude and long-distant recordings on soil nonlinearity, the nonlinear site coefficients are constrained by using a limited dataset. The coefficients of linear site scaling and deep soil effect are obtained with the full database. The period average of site-variability is found to be 0.43. The sigma decreases with decreasing the soil stiffness or increasing input rock motion. After employing residual analysis, the region-dependent correction coefficients for linear site scaling are also obtained.

Keywords: nonlinear site effects; deep soil effects; ground motion models

1. Introduction

The site amplification is defined as the ratio of ground-motion intensity measure (GMIM) at a site to the motion observed at reference rock-site condition [1]. One of the efficient procedures to compute site amplification is the application of the non-reference site amplification method [2]. In this method (e.g., [2–7]), ground-motion prediction equations (GMPEs) can be used to predict the ground-motion at reference rock-site condition and then normalize the empirically available GMIM to obtain site amplification.

Generally speaking, the current site amplification models impose three important soil behavior. The first one is the linear site response which is currently modeled with a continuous function of $V_{\rm S30}$ (time-based average of shear wave velocity of top 30 m soil media) after Boore et al. [8]. The site amplification is assumed to decrease linearly with increasing natural logarithm of $V_{\rm S30}$ [6–13]. Some researchers uses a period-independent fixed reference $V_{\rm S30}$ for linear scaling (e.g., 760 m/s in [12]) or period-dependent reference $V_{\rm S30}$ (e.g., [13]). Using either period-independent or dependent values does not affect the slope of linear site scaling [14]. Due to the low number of recordings at high $V_{\rm S30}$ sites, a constant amplification portion at the high $V_{\rm S30}$ values is preferred. Some model developers use period-dependent limiting $V_{\rm S30}$. At short periods, it reaches 1500 m/s and at longer periods, this value decreases to 400 m/s [15–17]. The period independent constraining value can be used as well (e.g., $V_{\rm S30} = 1000$ m/s in [7] or 1130 m/s in [18]). The second behavior in site amplification is soil nonlinearity, which is again modeled using $V_{\rm S30}$, which represents soil stiffness and input rock motion [6,7,9–13,15–21]. The level of soil nonlinearity decreases as soil stiffness increases or input rock motion decreases. The final behavior is the deep soil effect which is modeled with the depth to rock parameter (e.g., Z1, depth to VS profile reaches 1 km/s [21]).

Geosciences **2018**, *8*, 264 2 of 20

Another important site parameter is the fundamental site frequency, f_0 (e.g., [22,23]). Although the results might be changed for global data, for European data, Sandıkkaya and Akkar [24] show that the use of the V_{S30} - f_0 pair in site scaling leads a slight decrease the within-event sigma when it is compared with the V_{S30} -Z1 pair. As well, none of the reference databases (see next section) provides f_0 . Consequently, within the context of this study we cannot use f_0 as a site parameter.

There are two functional forms, which are discussed in the context of this study, to describe the soil nonlinearity. Zhoa et al. study [15] also proposed a functional form but it employs a predominant site period, so that it will not be elaborately discussed. The discussions related to previously published site models (e.g., [6,9–11,20]) can be found in detail in the Sandıkkaya et al. [7] study. The first functional form, proposed by Walling et al. [11], is generated by employing ground motion simulations and site response analysis. Sandıkkaya et al. [7] site model uses this functional form but computes the nonlinear coefficients with empirical data. Later, Kamai et al. [13] modified the Walling et al. study with an increasing number of simulations and site response analysis. The soil nonlinearity is formulated as a multiplication of the nonlinear site coefficient with a function including both input rock motion and soil stiffness. Chiou and Youngs [10] offered the second functional form which is also used by Seyhan and Steward [12] (SS14 or BSSA14, Boore et al. [17]—throughout the text we use them interchangeably but they refer the same site model) and Chiou and Youngs [19] (CY14). Contrary to the Walling et al. model, to compute the soil nonlinearity, the nonlinear site coefficient is multiplied with two functions: one including input rock motion and the other including V_{S30} . Application of the second functional form seems more practical, especially in computing the variability of site amplification in terms of either V_{S30} or input rock motion or both.

In this study, we consider linear and nonlinear site behaviors together with deep soil effect to simulate site amplification. In the following sections, we firstly give details about the strong-motion database that we use in the regressions. Secondly, a rock motion GMPE is generated to estimate the ground motion intensities at reference rock site condition. Thirdly, site amplification ratios are computed and the regressions are performed to obtain site model coefficients. Then, the site variability is expressed in terms of PSA_{rock} and V_{S30} . The paper continues with a comparison of the proposed model with some of the site models in the literature. Finally, we employ residual analysis to investigate the possible regional effects in the linear site response term.

2. Ground-Motion Database

A global strong-motion dataset is merged from the global NGA-West2 dataset [25], regional European datasets [26,27], and local Iran, Japanese and Turkish datasets [28–30]. The NGA-West2 database is composed of only five earthquakes from Japan (1925 records) and 119 earthquakes from Europe and the Middle East (524 records). Thus, the data from Europe, the Middle East and Japan in the NGA-West2 database was enhanced by local and regional databases. The database consists of stations with measured V_{S30} and accelerograms recorded within 300 km (Joyner-Boore distance, R_{JB} is used). The lower moment magnitude (M_w) limit of normal, reverse, and strike-slip earthquakes was 3.5. Only shallow crustal earthquakes with a maximum depth of 35 km are used. Finally, we used only events and stations with at least two recordings (only exceptions are made to $M_w + 6.75$ events recorded at soft sites with $V_{S30} < 360$ m/s, due to not losing any possible nonlinear site effects). Generally, in single-station sigma studies (e.g., [31]), at least 10 recordings per station was used. We cannot follow such criterion because if it were applied, most of the stations would be removed, as well as we would lose some records that might have possible nonlinear site effects.

We use eight larger seismic regions by following Flinn et al. [32]. The regions are listed in Table 1. Since there are only three events from Alaska and New Zealand regions, they are merged with earthquakes occurred in "Oregon, California and Nevada" region. Guam to Japan, Japan–Kuril Islands–Kamchatka Peninsula, Southwestern Japan and Ryukyu Islands, and Eastern Asia regions were labelled as Japan in the context of this study. The waveforms from western Caucasus and Armenia and Northern Italy were considered as western Asia and western Mediterranean areas, respectively.

Geosciences **2018**, 8, 264 3 of 20

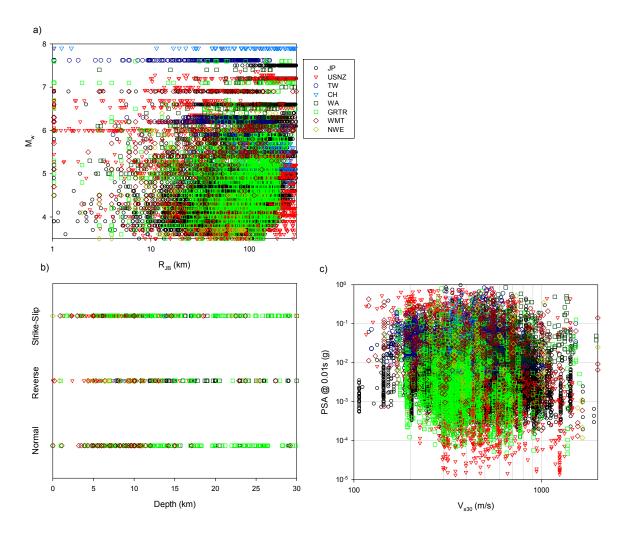


Figure 1. Seismological features of the database (**a**) R_{JB} - M_w scatters, (**b**) Depth vs. style-of-faulting, and (**c**) V_{S30} vs. PSA at T = 0.01 s. Note that the larger seismic regions are shown with the same color-code in each plot.

Table 1. Standard deviation model of the site model.

Larger Flinn-Engdahl Seismic Regions	Acronym		
Oregon, California and Nevada *	USNZ		
New Zealand Region	USNZ		
Guam to Japan	JP		
Japan-Kuril Islands-Kamchatka Peninsula	JP		
Southwestern Japan and Ryukyu Islands	JP		
Eastern Asia	JP		
Taiwan	TW		
Indıa-Xizang-Sichuan-Yunnan	CH		
Western Asia **	WA		
Middle East-Crimea-Eastern Balkans	TRGR		
Western Mediterranean area ***	WMT		
Northwestern Europe	NWE		

^{*} Including Alaska, ** Including western Caucasus and Armenia, *** Including northern Italy.

The database is composed of 20,070 waveforms from 1378 earthquakes recorded at 2134 stations. The seismological features of the database are presented in Figure 1. The M_w - R_{JB} distribution of the

Geosciences **2018**, *8*, 264 4 of 20

database is shown in Figure 1a for larger seismic regions used in this study. The database is dominated by low-magnitude and long-distant records. The distribution becomes sparse as the magnitude increases and distance decreases. The effect of the low number of such recordings on nonlinear site effects is discussed in the following section. Figure 1b shows the depth distribution of normal, reverse, and strike-slip earthquakes. Almost all types of earthquakes were well distributed for depths less than 15 km. This database also overcomes the drawbacks of NGA-West2 and RESORCE databases, which have a sufficiently low number of normal and reverse earthquakes, respectively. Figure 1c shows the distribution of PSA at T = 0.01 s versus $V_{\rm S30}$ of the database. The data was well sampled for stiff sites. The distribution loosened both in rock and very soft sites.

The geometric average of the two horizontal components was used. It is noted that, the NGA-West2 database gave orientation-independent spectral coordinates. For the waveforms provided in the PEER Strong Motion Database (peer.berkeley.edu.tr; last accessed: 17 October 2017), we computed the geometric average of the horizontal components. For the restricted waveforms, we apply period-dependent correction factors provided by Figure 4 of [33] to compute geometric average of waveforms from the given orientation-independent spectral ordinates. The period range of this study was limited to 4 s since we observed no significant nonlinearity beyond this period, as well as the number of records being decreased due to a usable period range (especially for the European data).

3. Ground Motion Prediction Equation for Rock Motion

A predictive model for GMIM at reference rock site condition which is represented by $V_{S30} = 760 \,\mathrm{m/s}$ was generated to compute site amplification values. The functional form used to compute the median natural logarithm of pseudo-spectral acceleration at 5% damping ratio, $ln(PSA_{rock})$ was composed of event scaling (magnitude scaling and style-of-faulting, SoF terms), distance scaling (geometric and anelastic attenuation terms), and site scaling (linear site response term) (Equations (1)–(7)). The regression coefficients and between-event residuals (η_i), between-site residuals (δ_j) and within-event residuals (ϵ_{ij}) were computed with the random-effects algorithm proposed by Bates et al. [34]. These residuals were assumed to have normal distributions with standard deviations of σ_e , σ_s and σ_w with the total variability of σ_t [35].

$$ln(PSA_{rock}) = f_{event} + f_{dist} + f_{dist,reg} + f_{event,reg} + f_{site} + \eta_i + \delta_j + \varepsilon_{ij}$$
(1)

$$f_{event} = \begin{cases} a_1 + a_2(M_w - 6.75) + a_4(M_w - 8.5)^2 + a_5F_N + a_6F_R \text{ for } M_w < 6.75\\ a_1 + a_3(M_w - 6.75) + a_4(M_w - 8.5)^2 + a_5F_N + a_6F_R \text{ for } M_w \ge 6.75 \end{cases}$$
 (2)

$$f_{dist} = a_7 \sqrt{R_o^2 + R_{JB}^2} + [a_8 + a_9(M_w - 6.75)] \sqrt{R_o^2 + R_{JB}^2}$$
 (3)

$$f_{dist,reg} = \Delta a_{7,CH} \sqrt{R_o^2 + R_{JB}^2} + \Delta a_{7,WA} \sqrt{R_o^2 + R_{JB}^2} + \Delta a_{7,WMT} \sqrt{R_o^2 + R_{JB}^2}$$
(4)

$$f_{event,reg} = \Delta a_{1,USNZ} + \Delta a_{1,CH} + \Delta a_{1,TW} + \Delta a_{1,WA} + \Delta a_{1,GRTR} + \Delta a_{1,WMT} + \Delta a_{1,NWE}$$
 (5)

$$f_{site} = a_{10} \ln \left[\frac{\min(1000, V_{S30})}{760} \right] \tag{6}$$

$$\sigma_t = \sqrt{\sigma_e^2 + \sigma_s^2 + \sigma_w^2} \tag{7}$$

We used a quadratic magnitude scaling with a break in the linear slope. The hinged magnitude that differentiates low-to-moderate and high-magnitude behavior was chosen as 6.75 by visual inspection of between-event residuals of events whose magnitudes were greater than 6.5. This magnitude scaling is also used in [21,36]. F_N and F_R are dummies to represent the style-of-faulting effects of normal and reverse events with respect to strike-slip events, respectively. The Joyner-Boore distance metric, R_{JB} was used in the regressions to surpass the hanging-wall effect as in Boore and Atkinson [9] predictive model. Both anelastic and geometric attenuation terms were included in distance scaling. The geometric

Geosciences **2018**, *8*, 264 5 of 20

attenuation term is magnitude dependent. The fictitious depth term, R_0 , was taken constant (10 km) in the regressions. The linear site response term with V_{S30} was employed and the site amplification for high V_{S30} values (1000 m/s) was constrained.

The regional effects were also included in the regressions to predict reference rock site estimates. After computing the regression coefficients for the global model, we inspected the between-event, between-site, and within-event residual distributions. For each region, we added a region-dependent constant to fix the biases observed in event and site terms. In distance scaling, the records from China, western Asia (e.g., Iran), and western Mediterranean (e.g., Italy) had biased estimates with the global model. They were removed by adding region-dependent anelastic attenuation constants. This was parallel to findings of NGA-West2 GMPEs [16–19]. However, we did not observe any trend in waveforms from Japan. One of the possible explanation could be that our database was dominated by records from this region.

The residual analysis for each independent variables was then performed. Figure 2 displays the between-event (top row) and within-event (bottom row) residual distributions for magnitude-and distance-scaling at T = 0.2 s (left panel) and T = 1 s (right panel), respectively. No major trends (or negligible trends) in these plots indicated that the performance of the GMPE was quite satisfactory. Although in short distances (R_{JB} < 20 km) the median estimations tended to be underestimated, at this stage of the study we did not apply any near-field correction. The between-site residuals were not shown in these plots, because they were very similar to the distribution observed in Figure 9 (please see the section entitled "Regional Effects").

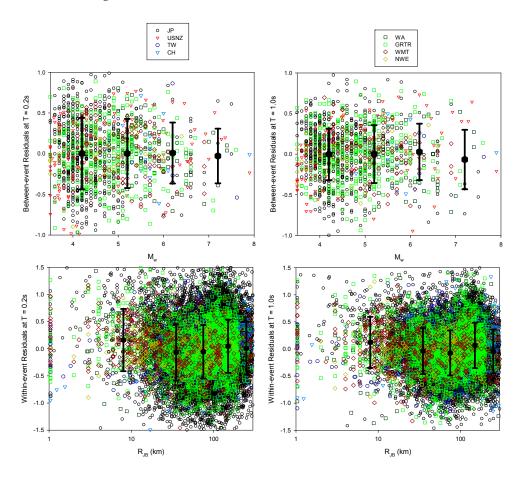


Figure 2. Between-event and within-event residual distributions of the reference rock motion predictive equations at T = 0.2 s (**left column**) and T = 1.0 s (**right column**). The same color-coding with Figure 1 is applied.

Geosciences **2018**, *8*, 264 6 of 20

4. Site Amplification Model

Initial attempts to compute the nonlinear site coefficients showed that they were sensitive to the database limits. The slope of linear site response increases when the database that was abundant in terms of low magnitude events or long-distant records was used. This yielded lower nonlinear coefficients (impose high nonlinearity) to capture the nonlinear site effects existing in the data. Thus, a two-step regression was applied to compute the model coefficients. At the first stage, the period-dependent site model coefficients were computed with a sub-database which was composed of only moderate to strong magnitude events ($M_w > 4.5$) recorded within 80 km. At the second stage (the full database is used), the nonlinear site coefficients were constrained from the first stage analysis; then the linear and deep soil coefficients were computed. A similar approach was also used in SS14.

Before presenting the proposed site model, the functional form given in SS14 (Equation (8)) was applied to the current study, and the findings were discussed. The model coefficients were γ_1 , γ_2 and γ_3 . The soil nonlinearity was computed with the multiplication of nonlinear site coefficient, γ_1 with the input rock motion term and soil stiffness term. In order to represent the seismic demand on rock, SS14 preferred peak ground acceleration at the rock site (PGA_{rock}) as an input parameter. They also fixed the γ_2 coefficient to 0.1 g, to fulfill a smooth transition in input rock-motion levels. The soil stiffness was expressed by an exponential function in terms of V_{S30} . This term is decreasing with increasing V_{S30} and for rock sites ($V_{S30} > 760 \text{ m/s}$) it becomes zero. The γ_3 coefficient was adapted from CY14 site model.

$$F_{nl} = \gamma_1 * ln \left[\frac{PGA_{rock} + \gamma_2}{\gamma_2} \right] * \left\{ \exp[\gamma_3(\min(V_{S30}, 760) - 360)] - \exp[400\gamma_3] \right\}$$
 (8)

We compared the linear and nonlinear site coefficients of Alternative I, which was computed by applying Equation (8) with PSA_{rock} at 0.01 s (by assuming PGA_{rock} is equal to PSA_{rock} at 0.01 s) to Alternative II which considers PSA_{rock} at 0.01 s and between-event residuals. The linear site coefficients with two alternatives were comparable (Figure 3a). The SS14 model had lower coefficients than both alternatives resulting in higher amplification. Alternative I yielded similar nonlinear coefficients with the SS14 model at the short-period range (0.1–0.5 s) where strong nonlinearity is observed (Figure 3b). However, the Alternative II that considers between-event residuals, imposed lesser soil nonlinearity in this interval period. The results from the Alternative II were more reliable. When employing non-reference site amplification method, the median estimate for rock motion from a GMPE could be overestimated or underestimated. Thus, this bias should be removed [19]. Since the influence of soil nonlinearity diminishes at longer periods, all coefficients were similar.

We then compared the use of PSA_{rock} at 0.01 s and PSA_{rock} (between-event residuals are taken into account) in the regressions, and negligible differences were observed in median site amplification estimates. Besides, the choice did not affect the site variability. This was parallel to findings of Sandıkkaya et al. [7] and Kamai et al. [13]. We preferred to continue with PSA_{rock} because it diminished the need to correlation coefficients between the period of interest and PSA_{rock} . This simplifies applications in the hazard analysis.

The soil stiffness term (V_{S30} -dependence) of the nonlinear functional form in SS14 site model linearly decreased with increasing logarithm of V_{S30} for soft sites having $V_{S30} < \sim 350$ m/s where nonlinearity was more pronounceable (Figure 3c). Instead of this formulation, we preferred to use a Gompertz sigmoid function. This function scales the soil nonlinearity linearly within a range of 200–400 m/s. This function is also capable of capping the rate of increase below 200 m/s. This enabled us to remove unwanted bias in very soft sites where the number of stations (or recordings) is limited.

Geosciences **2018**, *8*, 264 7 of 20

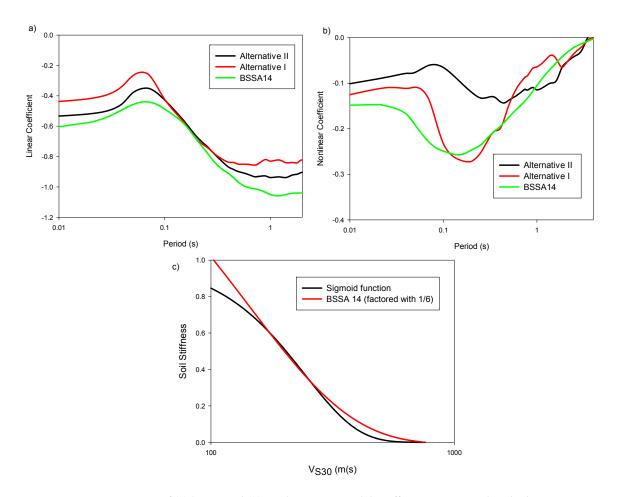


Figure 3. Comparison of (a) linear and (b) nonlinear site model coefficients computed with alternative functional forms. The coefficients given in BSSA14 are also included in these plots; (c) the soil stiffness term in the BSSA14 functional form and the proposed Gompertz sigmoid function are compared.

In the proposed soil model, the natural logarithm of site amplification, ln(Amp) consists of linear site scaling, deep soil effect, and soil nonlinearity (Equation (9)). The reference rock site condition is selected as V_{530} = 760 m/s and the site amplification was constrained for rock sites having V_{530} > 1000 m/s. The Z1 scaling of the proposed model was different from SS14 and CY14 site models. The deep soil effect was not considered in SS14 for periods shorter than 0.65 s. This period was 0.25 s in CY14 site model. In both models, the difference between measured and estimated Z1 values was used. However, Rodriguez-Marek et al. [30] study, which uses Z0.8 (depth at which shear-wave velocity attains 800 m/s), gives coefficients for shorter periods. The deep soil effect in the proposed model expressed in terms of the natural logarithm of the Z1 in meters. Since the number of stations with measured Z1 values is quite limited in the database, for the stations with unknown Z1 values, we employed V_{530} — Z1 relations given by CY14. Using estimated Z1 values in the regression did not cause any increase in between-site sigma. The period-independent b_4 and b_5 values were tuned before regression analysis to diminish the soil stiffness effect in high V_{530} values and constrain the soil nonlinearity at very soft sites.

$$\ln(Amp) = b_1 \ln\left[\frac{\min(1000, V_{S30})}{760}\right] + b_2 \ln[Z1] + b_3 \ln\left[\frac{exp[ln(PSA_{rock}) + \eta_i] + 0.1g}{0.1g}\right]$$

$$*exp\{-exp[b_4ln(V_{S30}) - b_5]\} + \delta_i + \varepsilon_{ii}$$
(9)

Geosciences **2018**, *8*, 264 8 of 20

The period-dependent standard deviation of between-site residuals, σ_s was found between 0.34 and 0.51. It was noted that this sigma value was obtained with the assumption of a homoscedastic model. This assumption was removed and how the variability of site amplification changes with V_{S30} and PSA_{rock} bins was investigated for T = 0.2 s and 1 s (Figure 4). The sites were grouped as very soft sites ($V_{S30} \le 200 \, \text{m/s}$), soft sites ($V_{S30} \le 300 \, \text{m/s}$), stiff sites ($V_{S30} \le 400 \, \text{m/s}$), moderate stiff sites ($V_{S30} \le 550 \, \text{m/s}$), very stiff sites ($V_{S30} \le 800 \, \text{m/s}$), and rock sites ($V_{S30} > 800 \, \text{m/s}$). We used $V_{S30} \le 550 \, \text{m/s}$) were weak motion, weak motion, moderate motion, strong motion, and very strong motion (please read the caption of Figure 4 for $V_{S30} \ge 100 \, \text{m/s}$).

At T = 0.2 s, the site-variability was the largest at very stiff sites. At T = 1.0 s, a similar trend was also observed. However, for rock sites, at both periods, variability was lower than very stiff sites. When compared to number of records at very stiff sites with those at rock sites, the first group had the larger number of records. This might be a reason for decreasing the sigma. The variability decreased from stiff sites to very soft sites. We should cap the variability at very soft sites because the rate of decrease might result in a very low standard deviation. As PSA_{rock} increases, the variability decreased, which is common in practice. Similar capping can also be made for lower and upper bounds of PSA_{rock} values. The V_{S30} and PSA_{rock} dependent site variability is given in (Equations (10)–(12)).

$$\sigma(V_{S30}, PSA_{rock}) = \sigma_s * c_0(c_1 * \ln(Y_{sig}) + c_2 * \ln(V_{Sig}))$$
(10)

$$Y_{sig} = \max(\min(0.35, PSA_{rock}), 0.005)$$
(11)

$$V_{Sig} = \max(\min(600, V_{S30}), 150)$$
(12)

where c_0 is the site variability constant and c_1 and c_2 represent the slope of PSA_{rock} and V_{S30} terms, respectively. The coefficients for the site model and standard deviation model are given in Table 2.

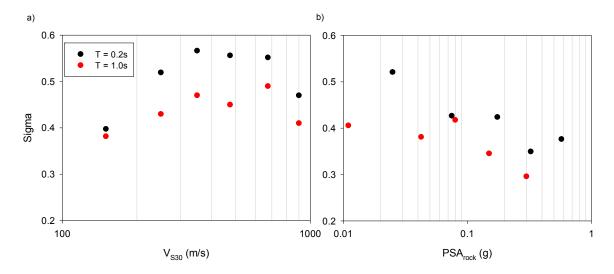


Figure 4. Variability of site amplification for T = 0.2 s and 1 s (a) for site bins (b) PSA_{rock} bins. The input rock motion bins for T = 0.2 s are: very weak motion ($PSA_{rock} < 0.05$ g), weak motion ($0.05 \le PSA_{rock} < 0.15$ g), moderate motion ($0.15 \le PSA_{rock} < 0.45$ g), strong motion ($0.45 \le PSA_{rock} < 0.75$ g), and very strong motion ($PSA_{rock} \ge 0.75$ g). For T = 1.0 s they are: very weak motion ($PSA_{rock} < 0.01$ g), weak motion ($PSA_{rock} < 0.05$ g), moderate motion ($PSA_{rock} < 0.05$ g), strong motion ($PSA_{rock} < 0.05$ g), and very strong motion ($PSA_{rock} < 0.05$ g).

The proposed site model is compared with the SS14 and CY14 site models. The nonlinear soil behavior of the proposed model is dominant at short periods and gradually diminishes after 1 s, and almost vanishes after 2.5 s. We did not observe any nonlinearity after 3 s. This was parallel to

Geosciences **2018**, *8*, 264 9 of 20

findings of SS14 and CY14 (e.g., SS14 had some nonlinearity after 3 s but their nonlinear coefficients were approximately zero).

Figure 5 shows the period dependency of site amplification estimations at $V_{\rm S30}$ = 180 m/s (very soft soil), $V_{\rm S30}$ = 360 m/s (stiff soil) and $V_{\rm S30}$ = 550 m/s (very stiff soil) for weak and strong input rock motion levels. At weak motion levels, our estimations were lower than estimates of the SS14 and CY14 site models, on the other hand, as input rock motion level increased due to the lower nonlinearity imposed in our model, our estimations became higher than SS14 and CY14 site models at short periods. Generally, the proposed model produced lower amplifications at long periods. The amplification estimations were very close to the SS14 and CY14 site models at very stiff sites. As sites get softer, the difference in amplification becomes more visible in this period interval. The observed differences are due to modeling approaches and database features (especially including more data from Japan) in the regressions.

Table 2. Site model coefficients. The period independent b_4 and b_5 are 2 and 11, respectively.

T (s)	b_1	b_2	<i>b</i> ₃	σ_s	c_0	c_1	c_2
				<u> </u>			
0.01	-0.53307	-0.46412	0.02105	0.47096	1.24013	0.09542	-0.05865
0.025	-0.50842	-0.3904	0.02023	0.47508	1.24682	0.09906	-0.05951
0.04	-0.45025	-0.31255	0.01858	0.48906	1.33552	0.12324	-0.06481
0.05	-0.38023	-0.23187	0.02029	0.50412	1.6779	0.18762	-0.08741
0.07	-0.3505	-0.18413	0.02376	0.50892	1.57403	0.12994	-0.0791
0.1	-0.42752	-0.37652	0.03221	0.49777	1.52282	0.12604	-0.07408
0.15	-0.55919	-0.53679	0.03248	0.47977	1.31863	0.11085	-0.05612
0.2	-0.6673	-0.6571	0.02956	0.46896	1.21025	0.10065	-0.04777
0.25	-0.73135	-0.69189	0.02516	0.45698	1.13978	0.07837	-0.03958
0.3	-0.7884	-0.68208	0.03152	0.45065	1.05645	0.04621	-0.03245
0.35	-0.8332	-0.69252	0.03233	0.44141	1.01481	0.05533	-0.02765
0.4	-0.8681	-0.74537	0.03521	0.43589	1.00182	0.05914	-0.02363
0.45	-0.88575	-0.73547	0.03923	0.42954	0.94803	0.06557	-0.0179
0.5	-0.89944	-0.69269	0.04159	0.42699	0.94724	0.06067	-0.0171
0.6	-0.91493	-0.6348	0.0458	0.41593	0.95504	0.07576	-0.01606
0.7	-0.93236	-0.63204	0.04993	0.40303	1.01362	0.08323	-0.01527
0.75	-0.93217	-0.6378	0.04989	0.40219	1.03634	0.08203	-0.01622
0.8	-0.92975	-0.65092	0.05114	0.39766	1.05807	0.08385	-0.01434
0.9	-0.92777	-0.57775	0.05266	0.38861	1.11036	0.09388	-0.01658
1	-0.93815	-0.60041	0.05421	0.3815	1.16634	0.09095	-0.01502
1.2	-0.93377	-0.56801	0.05576	0.36982	1.29484	0.08078	-0.01434
1.4	-0.93847	-0.48684	0.05782	0.35868	1.32222	0.08353	-0.00681
1.6	-0.92242	-0.40484	0.05645	0.35713	1.30431	0.07158	-0.00268
1.8	-0.91608	-0.29053	0.05615	0.34643	1.35426	0.07341	0
2	-0.90369	-0.18149	0.05307	0.34133	1.38763	0.0679	0
2.5	-0.89442	-0.04175	0.05954	0.3396	1.41986	0.08582	0
3	-0.87386	0	0.05596	0.35349	1.37795	0.10208	0
3.5	-0.8551	0	0.05469	0.35286	1.34678	0.07501	0
4	-0.8468	0	0.05469	0.36845	1.2583	0.05876	0

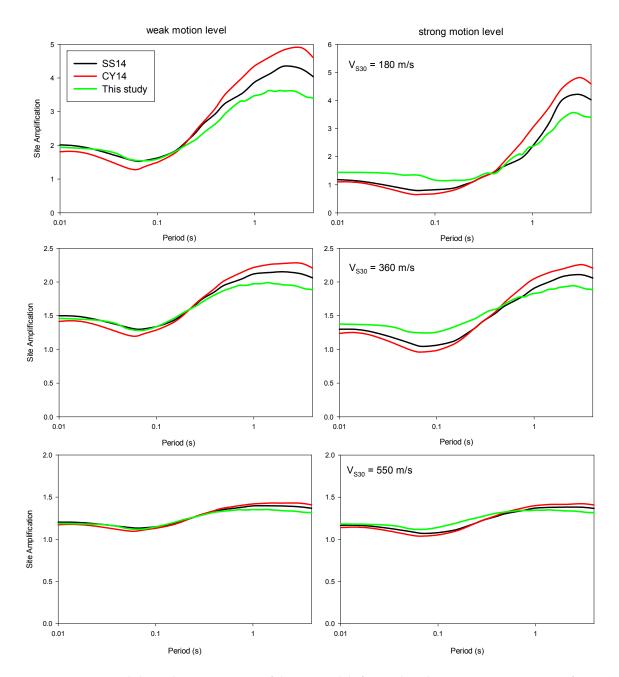


Figure 5. Period-dependent comparison of the site models for weak and strong motions in very soft soil ($V_{S30} = 180 \text{ m/s}$), soft soil ($V_{S30} = 360 \text{ m/s}$), and stiff soil ($V_{S30} = 550 \text{ m/s}$). Deep soil effect is not included in the plots.

Figures 6 and 7 compare the PSA_{rock} and V_{S30} dependence of site amplification at 0.2 s (right column) and 1.0 s (left column), respectively. In Figure 6, three site conditions ($V_{S30} = 150 \, \text{m/s}$, 255 m/s and 450 m/s) were considered. We selected weak, moderate and strong PSA_{rock} for the comparisons in Figure 7 (read the figure caption for the PSA_{rock} values). At T = 0.2 s, the site amplification estimations of the proposed model matched with the SS14 and CY14 site models at low seismic demands. As PSA_{rock} increases, our model tended to estimate lower amplification demonstrating less soil nonlinear behavior. At $V_{S30} = 450 \, \text{m/s}$, although CY14 and SS14 models had some nonlinearity, the proposed model was not very sensitive to PSA_{rock} . At T = 1 s, for stiff sites, amplifications were generally lower than the CY14 site model. Due to the lower nonlinear site behavior of our model, as PSA_{rock} increased, the amplification became higher when compared to the

SS14 site model. For the $V_{\rm S30}$ -scaling of the proposed model, SS14 and CY14 site models were similar at stiff site condition. However, as $V_{\rm S30}$ decreased the differences became more prominent. The 1 s amplification was matched with the SS14 site model, with both models producing lower amplification when compared to the CY14 site model.

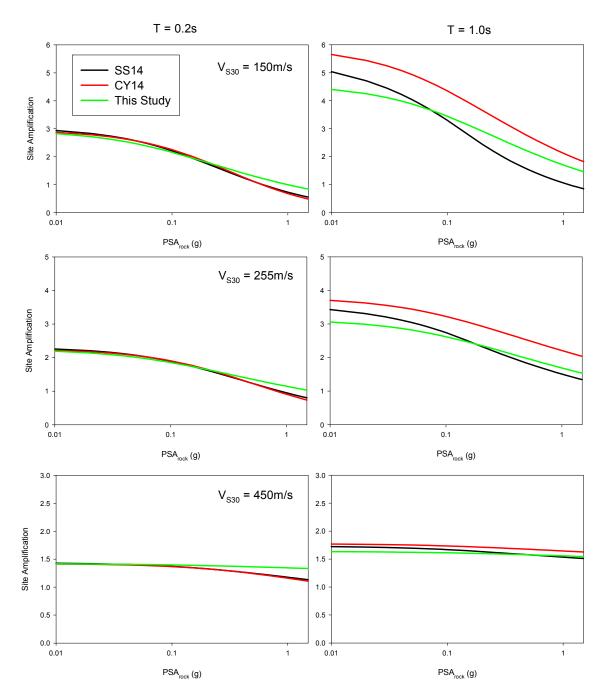


Figure 6. The comparison of the site models for very soft soil ($V_{S30} = 150$ m/s), soft soil ($V_{S30} = 255$ m/s), and stiff soil ($V_{S30} = 450$ m/s) at 0.2 s and 1.0 s. Deep soil effect is not included in the plots.

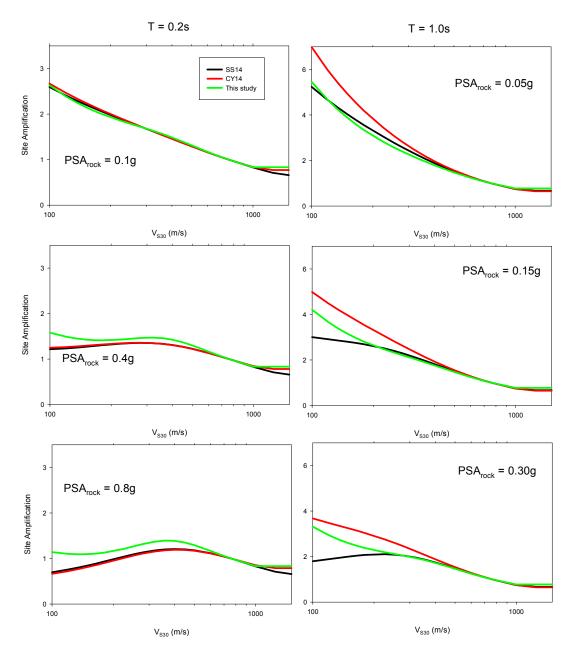


Figure 7. The comparison of the site models for weak, moderate, and strong input rock levels at 0.2 s and 1.0 s. Weak motion ($PSA_{rock@T0.2s} = 0.1$ g, $PSA_{rock@T1.0s} = 0.05$ g), moderate motion ($PSA_{rock@T0.2s} = 0.4$ g, $PSA_{rock@T1.0s} = 0.15$ g), and strong motion ($PSA_{rock@T0.2s} = 0.8$ g, $PSA_{rock@T1.0s} = 0.30$ g). Deep soil effect is not included in the plots.

5. Regional Effects

Within the context of this study, it was assumed that the nonlinear site and deep basin effects are region-independent. That is, if an amplification trend from one region is different from another, it is because of linear site response. The average of between-site residuals for each region were less than 1% because of application of region-dependent constants in the rock GMPE, and these biases are found to be statistically insignificant. Yet, this analysis did not provide any information about regional V_{530} scaling. To do so, we added a region-dependent correction factor, c_k , to the linear site term (Equation (13)).

$$g_{lin} = (b_1 + c_k) \ln \left[\frac{\min(V_{S30}, 1000)}{760} \right]$$
 (13)

We applied a significance level of 0.05 to test to the c_k values to determine whether the regional site amplification scaling was similar to the global site amplification trend or not. That is, the hypothesis c_k was equal to zero is tested for each region. Figure 8a shows the test results. The site amplification trend for CH (the acronyms for each region is given in Table 1) was found to be statistically insignificant whereas the hypothesis is rejected for WA in all period range. At only one or two periods, the slopes were found to be statistically significant for GRTR, WMT and NWE regions. These results for these regions were thus not given in Figure 8a. For periods lower than 0.1 s, the test results for region-dependent V_{S30} -scaling of TW sites indicated that different slopes to the global model should be used. At periods of 3 s to 4 s, both TW and JP had significant different slopes. At short periods (0.2–0.8 s), TW, JP, and USNZ slopes were found to be statistically significant. We give all c_k values in Table 3 but the statistically significant ones are highlighted with bold font. The period variation of the correction factor is shown in Figure 8b.

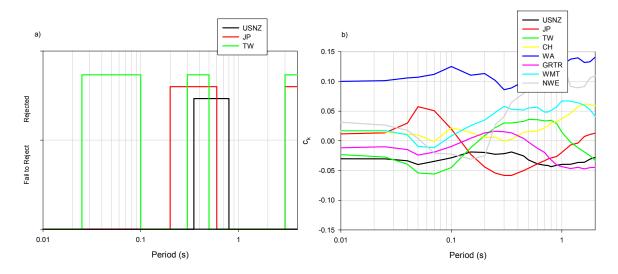


Figure 8. (a) The significance test results for USNZ, JP and TW, (b) the c_k for each region.

Figure 9 shows regionally corrected between-site residuals at T=0.2 s (left panel) and T=1.0 s (right panel) for each region (from top to bottom: USNZ, JP, TW, CH, WA, GRTR, WMT, and NWE). The between-site residuals were almost uniformly distributed. We classified the stations as very soft, soft, stiff, very stiff, and rock sites. The average of between-sites residuals of each group is also shown with its standard deviation in these plots. The very soft and rock sites from JP and WMT were underestimated at T=0.2 s. Due to the low number of stations in some bins (e.g., WA very soft sites, TW stiff sites and CH very stiff sites at T=1 s), biases were observed. Nevertheless, for each region, the residuals generally show no major trend.

T (s)	$c_{k,USNZ}$	$c_{k,JP}$	$c_{k,TW}$	$c_{k,CH}$	$c_{k,WA}$	$c_{k,GRTR}$	$c_{k,WMT}$	$c_{k,NWE}$
0.01	-0.0302	0.0117	-0.0233	0.0158	0.1001	-0.0118	0.0172	0.0314
0.025	-0.0303	0.0135	-0.0272	0.015	0.1013	-0.01	0.0174	0.0264
0.04	-0.0336	0.0298	-0.0394	0.0111	0.1059	-0.0148	0.0101	0.0178
0.05	-0.04	0.0575	-0.0541	0.0099	0.1071	-0.024	-0.0093	0.0038
0.07	-0.0346	0.0508	-0.056	-0.0012	0.1119	-0.019	-0.0114	-0.0206
0.1	-0.0287	0.0199	-0.045	0.022	0.1251	-0.0095	0.0084	-0.0222
0.15	-0.0187	-0.0228	-0.0114	0.0143	0.1105	0.0044	0.0258	-0.0307
0.2	-0.0196	-0.0439	0.0089	0.0056	0.1134	0.0133	0.035	-0.0254

Table 3. Site model coefficients for regional effects.

 Table 3. Cont.

T (s)	$c_{k,USNZ}$	$c_{k,JP}$	$c_{k,TW}$	$c_{k,CH}$	$c_{k,WA}$	$c_{k,GRTR}$	$c_{k,WMT}$	$c_{k,NWE}$
0.25	-0.0227	-0.0543	0.0222	0.0059	0.1016	0.0162	0.048	0.0274
0.3	-0.0216	-0.0583	0.03	-0.00003	0.086	0.0153	0.058	0.0407
0.35	-0.0187	-0.0583	0.0301	0.0025	0.089	0.0135	0.0534	0.065
0.4	-0.0239	-0.0544	0.0313	0.008	0.09462	0.007	0.05177	0.0728
0.45	-0.0254	-0.0502	0.0327	0.0142	0.0999	0.0041	0.0519	0.0798
0.5	-0.0322	-0.0461	0.036	0.0156	0.1073	-0.0022	0.0553	0.0879
0.6	-0.0388	-0.0389	0.0356	0.0163	0.1209	-0.0125	0.0565	0.0978
0.7	-0.0411	-0.0333	0.0336	0.022	0.1246	-0.0197	0.0483	0.1104
0.75	-0.0416	-0.0305	0.0339	0.0252	0.1224	-0.0269	0.0485	0.1166
0.8	-0.0436	-0.0289	0.0346	0.0297	0.1244	-0.0321	0.0512	0.1193
0.9	-0.0412	-0.0262	0.0289	0.0325	0.1239	-0.0408	0.0574	0.1303
1	-0.0397	-0.0195	0.0146	0.0375	0.1273	-0.0434	0.0673	0.1369
1.2	-0.0395	-0.0071	-0.0025	0.0463	0.1376	-0.0467	0.0668	0.0914
1.4	-0.0365	-0.0036	-0.0115	0.0574	0.1397	-0.0446	0.064	0.0893
1.6	-0.0361	0.0073	-0.0188	0.062	0.1319	-0.0473	0.06	0.0914
1.8	-0.0307	0.0108	-0.0252	0.0609	0.1332	-0.0452	0.0523	0.1062
2	-0.028	0.0129	-0.0328	0.0591	0.1408	-0.0445	0.041	0.1092
2.5	-0.0336	0.0277	-0.0413	0.0588	0.1471	-0.0316	0.0197	0.0509
3	-0.0325	0.0369	-0.0579	0.0566	0.1679	-0.0268	0.0138	0.105
3.5	-0.0272	0.0461	-0.063	0.0525	0.1422	-0.0294	0.0216	0.156
4	-0.0203	0.0503	-0.0641	0.0572	0.1945	-0.0242	0.0138	0.2198

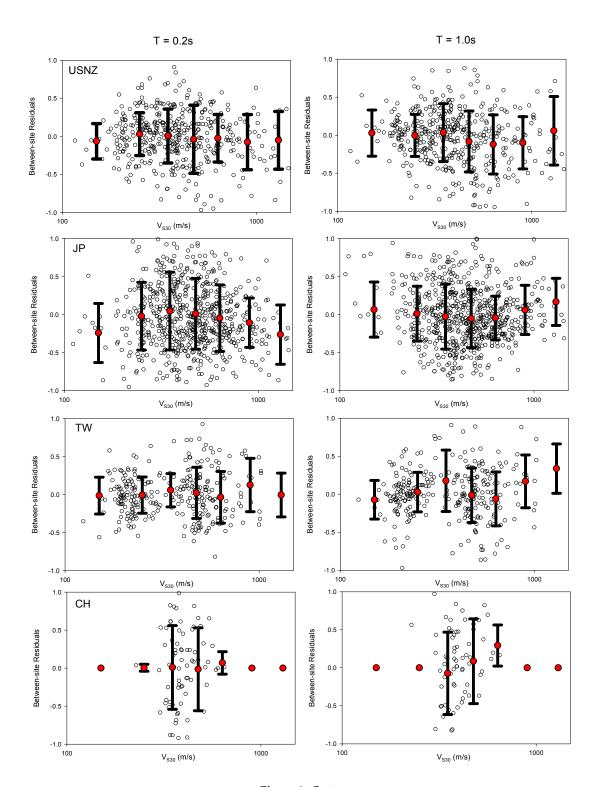


Figure 9. Cont.

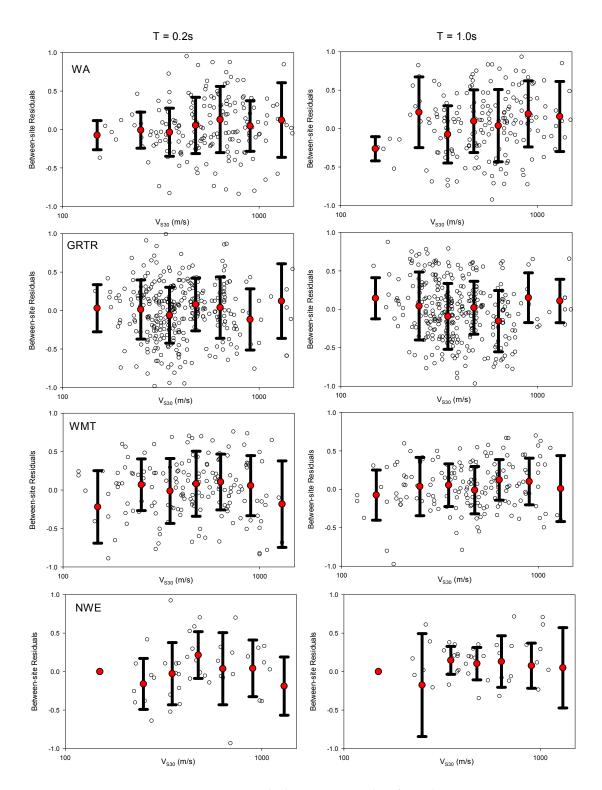


Figure 9. Between-site residuals at T = 0.2 s and 1 s for each region.

The variability of site amplification (computed by observed PSA value divided by estimated PSA_{rock} and between-event residuals) for each region is plotted for V_{S30} (left panel) and PSA_{rock} (right panel) bins for T = 0.2 s (top row) and T = 1.0 s (bottom row) in Figure 10. The intervals of V_{S30} and PSA_{rock} are given in the figure caption. The regional variability also had a wide range for both V_{S30} and PSA_{rock} bins. For example, soft-soil site standard deviation was 0.2 and 0.55 for the TW region and JP region, respectively. Rock-site standard deviation was generally lower than very stiff site

sigma. There is a decreasing trend from very stiff sites to very soft sites. However, for some regions this observation did not hold, with larger variability being computed at very soft sites. The similar observation for PSA_{rock} could also be made. The fact that the site bins did not have uniform station distribution, and also an unbalanced number of recordings (besides not uniform magnitude distance scatters) for each region, were the main reasons for violating the general observation.

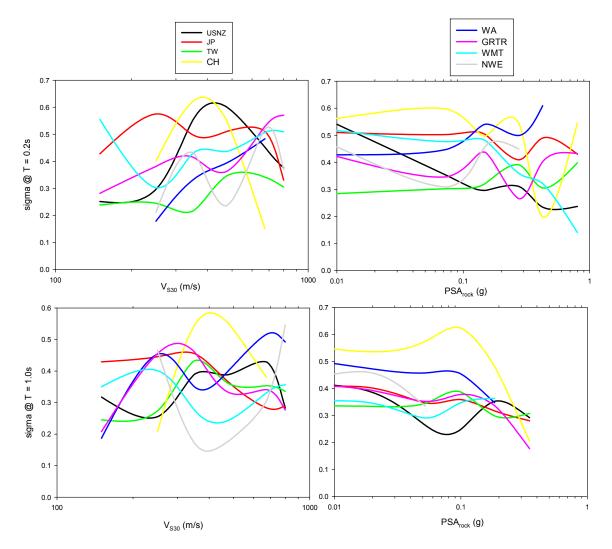


Figure 10. Variability of site amplification for V_{S30} and PSA_{rock} at T = 0.2 s and 1.0 s. The site bins are: very soft sites ($V_{S30} \leq 200 \text{ m/s}$), soft sites ($200 < V_{S30} \leq 300 \text{ m/s}$), stiff sites ($300 < V_{S30} \leq 400 \text{ m/s}$), moderate stiff sites ($400 < V_{S30} \leq 550 \text{ m/s}$), very stiff sites ($550 < V_{S30} \leq 800 \text{ m/s}$), and rock sites ($V_{S30} > 800 \text{ m/s}$). The input rock motion bins for T = 0.2 s are: very weak motion ($PSA_{rock} < 0.05 \text{ g}$), weak motion ($0.05 \leq PSA_{rock} < 0.15 \text{ g}$), moderate motion ($0.15 \leq PSA_{rock} < 0.45 \text{ g}$), strong motion ($0.45 \leq PSA_{rock} < 0.75 \text{ g}$), and very strong motion ($PSA_{rock} \geq 0.75 \text{ g}$). For T = 1.0 s they are: very weak motion ($PSA_{rock} < 0.01 \text{ g}$), weak motion ($PSA_{rock} < 0.01 \text{ g}$), weak motion ($0.01 < PSA_{rock} < 0.05 \text{ g}$), moderate motion ($0.05 < PSA_{rock} < 0.10 \text{ g}$), strong motion ($0.10 < PSA_{rock} < 0.20 \text{ g}$), and very strong motion ($PSA_{rock} > 0.20 \text{ g}$).

6. Conclusions

In this study, we propose a new nonlinear site amplification model that also considers the deep soil effect. A global database composed of records from western United States, Japan, Taiwan, China, New Zealand, Iran, Turkey, Greece, Italy, Switzerland, and France is used to compute site model coefficients. The functional form of the proposed site model is adopted from SS14 and CY14 site models. The proposed model makes use of soil stiffness and level of input rock motion to describe the soil

nonlinear behavior. We refine the exponential functional form to define soil stiffness with a Gompertz function that restricts the nonlinear behavior at low-velocity sites. The agreement between the site amplification estimations with the SS14 and CY14 models and the unbiased residual distributions advocate the reliability of the proposed site model. The variability of the site model is expressed in terms of V_{S30} and PSA_{rock} . As sites get softer or PSA_{rock} increases, the variability of the site amplification decreases. This study also focused on the regional differences in site effects. Regional differences are found to be statistically insignificant for CH, GRTR, WMT, and NWE. However, the site amplification observed in WA, USNZ, JP, and TW are different from the global V_{S30} -scaling.

The soil nonlinearity is found to be lower than previous site models. One of the possible reasons is that we use a large database but the number of records with nonlinear site effects is limited. Besides, using a lower number of records per station resulted in a higher sigma than previous studies. These drawbacks can be solved by merging the features of the empirically derived site models with simulation-based site amplification studies (e.g., Kamai et al. [13]).

It is recommended that the applicability the model extends to $150 < V_{S30} < 1200$ m/s. The proposed site model can be served as a site-scaling term in the future ground motion prediction equations. We also emphasize that when it is the case, only nonlinear site coefficients should be used and the coefficients for linear site response and deep soil effects should be computed in the regression steps. The site model can also be considered as a candidate site model in the computation of the regional site factors for seismic design codes (e.g., [37]).

Author Contributions: This study is a part of L.D.D's MS thesis.

Funding: This study is funded by The Scientific and Technical Research Council of Turkey (TUBITAK) under Project No: 117M146.

Acknowledgments: The grant provided by TUBITAK is appreciated. The authors express their sincere gratitude to two anonymous reviewers.

Conflicts of Interest: The authors declare no conflict of interest.

References

- 1. Borcherdt, R.D. Effects of Local Geology on Ground Motion near San Francisco Bay. *Bull. Seismol. Soc. Am.* **1970**, *60*, 29–61.
- 2. Stewart, J.P.; Liu, A.H.; Choi, Y. Amplification Factors for Spectral Acceleration in Tectonically Active Regions. *Bull. Seismol. Soc. Am.* **2003**, *93*, 332–352. [CrossRef]
- 3. Field, E.H. A modified ground-motion attenuation relationship for southern California that accounts for detailed site classification and a basin-depth effect. *Bull. Seismol. Soc. Am.* **2000**, *90*, S209–S221. [CrossRef]
- 4. Lee, Y.; Anderson, J.G. Potential for improving ground-motion relations in southern California by incorporating various site parameters. *Bull. Seismol. Soc. Am.* **2000**, *90*, S170–S186. [CrossRef]
- 5. Steidl, J.H. Site response in southern California for probabilistic seismic hazard analysis. *Bull. Seismol. Soc. Am.* **2000**, 90, S149–S169. [CrossRef]
- 6. Choi, Y.; Stewart, J.P. Nonlinear Site Amplification as Function of 30 m Shear Wave Velocity. *Earthq. Spectra* **2005**, *21*, 1–30. [CrossRef]
- 7. Sandıkkaya, M.A.; Akkar, S.; Bard, P.Y. A Nonlinear Site-Amplification Model for the Next Pan-European Ground-Motion Prediction Equations. *Bull. Seismol. Soc. Am.* **2013**, *103*, 19–32. [CrossRef]
- 8. Boore, D.M.; Joyner, W.B. Site Amplifications for Generic Rock Sites. Bull. Seismol. Soc. Am. 1997, 87, 327–341.
- 9. Boore, D.M.; Atkinson, G.M. Ground-Motion Prediction Equations for the Average Horizontal Component of PGA, PGV, and 5%-Damped PSA at Spectral Periods between 0.01 s and 10.0 s. *Earthq. Spectra* **2008**, 24, 99–138. [CrossRef]
- 10. Chiou, B.S.J.; Youngs, R.R. An NGA Model for the Average Horizontal Component of Peak Ground Motion and Response Spectra. *Earthq. Spectra* **2008**, *24*, 173–215. [CrossRef]
- 11. Walling, M.; Silva, W.; Abrahamson, N. Nonlinear Site Amplification Factors for Constraining the NGA Models. *Earthq. Spectra* **2008**, *24*, 243–255. [CrossRef]

12. Seyhan, E.; Stewart, J.P. Semi-Empirical Nonlinear Site Amplification from NGA-West2 Data and Simulations. *Earthq. Spectra* **2014**, *30*, 1241–1256. [CrossRef]

- 13. Kamai, R.; Abrahamson, N.A.; Silva, W.J. Nonlinear Horizontal Site Amplification for Constraining the NGA-West2 GMPEs. *Earthq. Spectra* **2014**, *30*, 1223–1240. [CrossRef]
- 14. Salic, R.; Sandıkkaya, M.A.; Milutinovic, Z.; Gulerce, Z.; Duni, L.; Kovacevic, V.; Markusic, S.; Mihaljevic, J.; Kuka, N.; Kaludjerovic, N.; et al. Reply to "Comment to BSHAP project strong ground motion database and selection of suitable ground motion models for the Western Balkan Region" by Carlo Cauzzi and Ezio Faccioli. *Bull. Earthq. Eng.* 2017, 15, 1349–1353. [CrossRef]
- 15. Abrahamson, N.A.; Silva, W.J.; Kamai, R. Summary of the ASK14 ground motion relation for active crustal regions. *Earthq. Spectra* **2014**, *30*, 1025–1055. [CrossRef]
- 16. Boore, D.M.; Stewart, J.P.; Seyhan, E.; Atkinson, G.M. NGA-West2 Equations for Predicting PGA, PGV, and 5% Damped PSA for Shallow Crustal Earthquakes. *Earthq. Spectra* **2014**, *30*, 1057–1085. [CrossRef]
- 17. Campbell, K.W.; Bozorgnia, Y. NGA-West2 ground motion model for the average horizontal components of PGA, PGV, and 5%-damped linear acceleration response spectra. *Earthq. Spectra* **2014**, *30*, 1087–1115. [CrossRef]
- 18. Chiou, B.S.J.; Youngs, R.R. Update of the Chiou and Youngs NGA Model for the Average Horizontal Component of Peak Ground Motion and Response Spectra. *Earthq. Spectra* **2014**, *30*, 1117–1153. [CrossRef]
- 19. Abrahamson, N.A.; Silva, W.J. Empirical Response Spectral Attenuation Relations for Shallow Crustal Earthquakes. *Seismol. Res. Lett.* **1997**, *68*, 94–127. [CrossRef]
- 20. Zhao, J.X.; Hu, J.S.; Jiang, F.; Zhou, J.; Rhoades, D.A. Nonlinear site models derived from 1-D analyses for ground-motion prediction equations using site class as the site parameter. *Bull. Seismol. Soc. Am.* **2015**, 105, 2010–2022. [CrossRef]
- 21. Abrahamson, N.A.; Silva, W. Summary of the Abrahamson and Silva NGA ground motion relations. *Earthq. Spectra* **2008**, *24*, 67–98. [CrossRef]
- 22. Cadet, H.; Bard, P.-Y.; Rodriguez-Marek, A. Defining a standard rock site: Propositions based on the KiK-net database. *Bull. Seismol. Soc. Am.* **2010**, *100*, 172–195. [CrossRef]
- 23. Hassani, B.; Atkinson, G.M. Applicability of the site fundamental frequency as a VS 30 proxy for central and eastern North America. *Bull. Seismol. Soc. Am.* **2016**, *106*, 653–664. [CrossRef]
- 24. Sandıkkaya, M.A.; Akkar, S. A Detailed Investigation on Akkar et al. (2013) pan-European Ground-Motion Prediction Equations and Proposals for Future Versions. In Proceedings of the 2nd European Conference on Earthquake Engineering and Seismology, Istanbul, Turkey, 24–29 August 2014.
- 25. Ancheta, T.D.; Darragh, R.B.; Stewart, J.P.; Seyhan, E.; Silva, W.J.; Chiou, B.S.J.; Wooddell, K.E.; Graves, R.W.; Kottke, A.R.; Boore, D.M.; et al. NGA-West2 Database. *Earthq. Spectra* **2014**, *30*, 989–1005. [CrossRef]
- Akkar, S.; Sandıkkaya, M.A.; Şenyurt, M.; Sisi, A.A.; Ay, B.Ö.; Traversa, P.; Douglas, J.; Cotton, F.; Luzi, L.; Hernandez, B.; et al. Reference Database for Seismic Ground-Motion in Europe (RESORCE). *Bull. Earthq. Eng.* 2014, 12, 311–339. [CrossRef]
- 27. Luzi, L.; Puglia, R.; Russo, E.; Orfeus, W.G. *Engineering Strong Motion Database*, version 1.0.; Istituto Nazionale di Geofisica e Vulcanologia, Observatories & Research Facilities for European Seismology: Milano, Italy, 2016.
- 28. Kale, Ö.; Akkar, S.; Ansari, A.; Hamzehloo, H. A ground-motion predictive model for Iran and Turkey for horizontal PGA, PGV and 5%-damped response spectrum: Investigation of possible regional effects. *Bull. Seismol. Soc. Am.* **2015**, *105*, 963–980. [CrossRef]
- 29. Dawood, H.M.; Rodriguez-Marek, A.; Bayless, J.; Goulet, C.; Thompson, E. A Flatfile for the KiK-net Database Processed Using an Automated Protocol. *Earthq. Spectra* **2016**, *32*, 1281–1302. [CrossRef]
- 30. Sandıkkaya, M.A.; Aghaalipour, N.; Gülerce, Z. Türkiye kuvvetli yer hareketi veri tabaninin genişletilmesi: Bir ön çalişma. In Proceedings of the 4th International Conference on Earthquake Engineering and Seismology, Eskişehir, Turkiye, 11–13 October 2017. (In Turkish)
- 31. Rodriguez-Marek, A.; Montalva, G.A.; Cotton, F.; Bonilla, F. Analysis of single-station standard deviation using the KiK-net data. *Bull. Seismol. Soc. Am.* **2011**, *101*, 1242–1258. [CrossRef]
- 32. Flinn, E.A.; Engdahl, E.R.; Hill, A.R. Seismic and Geographical Regionalization. *Bull. Seismol. Soc. Am.* **1974**, 64, 771–992.
- 33. Boore, D.M. Orientation-independent, non geometric-mean measures of seismic intensity from two horizontal components of motion. *Bull. Seismol. Soc. Am.* **2010**, *100*, 1830–1835. [CrossRef]
- 34. Bates, D.M.; Maechler, M.; Bolker, B. Lme4: Linear Mixed-Effects Models Using S4 Classes, R Manual, 2013. Available online: http://CRAN.R-project.org/package=lme4 (accessed on 8 December 2016).

Geosciences **2018**, *8*, 264 20 of 20

35. Al Atik, L.; Abrahamson, N.; Bommer, J.J; Scherbaum, F.; Cotton, F.; Kuehn, N. The variability of ground motion prediction models and its components. *Seismol. Res. Lett.* **2010**, *81*, 794–801. [CrossRef]

- 36. Akkar, S.; Sandıkkaya, M.A.; Bommer, J.J. Empirical ground-motion models for point- and extended-source crustal earthquake scenarios in Europe and the Middle East. *Bull. Earthq. Eng.* **2014**, *12*, 359–387. [CrossRef]
- 37. Sandıkkaya, M.A.; Akkar, S.; Bard, P.Y. A probabilistic procedure to describe site amplification factors for seismic design codes. *Soil Dyn. Earthq. Eng.* **2018**. [CrossRef]



© 2018 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (http://creativecommons.org/licenses/by/4.0/).